









Cultural Transposition and the Semiosphere: tools for analysing mathematical discourse

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Gender Gap in Mathematics

The findings:

- "[...] show that the gender difference are very small and negligible in general. However, variations were observed in the magnitude of the differences across different nations. This provides further evidence for the malleable nature of the existing gender differences in mathematics."
- "[...] revealed an increase in the gender gap from fourth grade to the eighth grade. Although the increase was relatively small, and the differences were still negligible, it could be a representation of an ascending trend in gender differences as students grow and get closer to the final years of compulsory education."
- "[...] imply that more gender parities in social, educational, economic, and health standards did not lead to less gender distinctions in attitudes towards mathematics (in a number of European countries) and less gender parities in those standards did not lead to more gender differences, as in the case of Middle Eastern nations. Moreover, this implication further illustrates the significance of regional differences and motivational patterns in cross-cultural studies."

(Ghasemi & Burley, 2019)



«Teaching methods gap» in Mathematics

(Stigler & Hiebert, 1999)

[...] Looking across cultures is one of the best ways to see beyond the blinders and sharpen our view of ourselves. [...] we were struck by the homogeneity of teaching methods within each culture, compared with the marked differences in methods across cultures. Readers who are parents will know that there are differences among American teachers; they might even have fought to move their child from one teacher's class into another teacher's class. Our point is that these differences, which appear so large within our culture, are dwarfed by the gap in general methods of teaching that exist across cultures.

We are not talking about a gap in teachers' competence but about a gap in teaching methods. These cross-cultural differences in methods are instructive because they allow us to see ourselves in new ways.

[...] In our view, teaching is the next frontier in the continuing struggle to improve schools.









The culturally sensitive understanding in Mathematics



Mathematics as a DISCOURSE



Sfard, A., & Linchevski, L. (1994). The gains and the pitfalls of reification—the case of algebra. In *Learning mathematics* (pp. 87-124). Springer, Dordrecht.



The culturally sensitive understanding in Mathematics



Learning mathematics could be defined as "individualizing mathematical discourse, that is, as the process of **becoming able** to have mathematical communication".

[...] by learning to participate in increasingly complex types of discourse of an increasingly complex degree of difficulty: where the mathematical content (the mathematical object) may still be the same, but the discourse about it evolves.

(Kim, Ferrini-Mundy & Sfard, 2012)



"Verbal shapes?

Let us think about this first in English. Shape is expressed in many ways."

(Barton, 2008, p. 28)















The noun form is privileged in English;

it seems to be the base concept in everyday language and in mathematical discourse. [...] We can draw a pentagon, and something may be pentagonal, but it sounds clumsy to ask someone to "pentagonalise a piece of paper".

[...] In Navajo the opposite is the case:

A basic characteristic of the Navajo world view ... is the **fundamentally dynamic or active nature** of the world and everything in it. ... [This is a] **basic perspectival difference from Western thought and language.** (Pinxten et al., 1983, p. 15,

in Barton, 2008, p. 28-28)



"The mathematician in me is intrigued by the **idea of verbal expression of shapes**.

Could this make a difference mathematically?

Does the way we think about the idea of triangularity affect what we understand about it? [...] How might geometry be different?

Let me be clear that this is my mind-game, not a Navajo mind-game. The way I am using the idea of «circle as an action» is my conception of that idea, not a Navajo one."

(Barton, 2008, p. 29)









Imagine, then, that circularity is an action, not an object, thus we must talk about **circling**, not a circle. What do you think/do?













One major difference between turtle geometry and coordinate geometry rests on the notion of the *intrinsic* properties of geometric figures. An intrinsic property is one which depends only on the figure in question, not on the figure's relation to a frame of reference. (Turtle Geom., p. 13)









Culturally sensitive tools in Mathematics Education



The Cultural Transposition

Cultural transposition: Italian didactic experiences inspired by Chinese and Russian perspectives on whole number arithmetic

Maria Mellone, Alessandro Ramploud, Benedetto Di Paola & Francesca Martignone



"This **is not about comparative** philosophy, about paralleling different conceptions, but about a philosophical dialogue in which every thought, when coming towards the other, **questions itself about its own unthought**." (Jullien 2006, p. 8)

The Cultural Transposition is a process activated by researchers, educators, and teachers. **Through the contact with** educational practices of **other cultural contexts**, they **reconsider the issues of educational intentionality** in educational practice of one's own cultural context, which is the background of any educational practice."





The SEMIOSPHERE

Asymmetry

Explosion









International Day of Women and Girls in Science



Rongjin Huang Akihiko Takahashi João Pedro da Ponte *Editors*

Theory and Practice of Lesson Study in Mathematics

TIMSS 1999

An International Perspective

World Association of Lesson Studies

https://www.walsnet.org/

Il lesson study per la formazione degli insegnanti

A cura di Maria G. Bartolini Bussi e Alessandro Ramploud





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"...each language contains its own mathematical world.

The worlds may be implicit, of small scope, and/or undeveloped, but these worlds exist—they are not just rudimentary versions of conventional mathematics [...].

These worlds represent systems of meaning concerned with quantity, relationships, or space, and are, in some sense, incommensurable with NUC-mathematics." = Near-Universal, Conventional Mathematics





(Barton, 2008, p. 144)









